VIDYA BHAWAN BALIKA VIDYA PITH

शक्तिउत्थानआश्रमलखीसरायबिहार

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In each of the following Exercise 1 to 5, find the equation of the circle with

1. Centre (0, 2) and radius 2

Solution:

Given:

Centre (0, 2) and radius 2

Let us consider the equation of a circle with centre (h, k) and

Radius r is given as $(x - h)^2 + (y - k)^2 = r^2$

So, centre (h, k) = (0, 2) and radius (r) = 2

The equation of the circle is

$$(x-0)^2 + (y-2)^2 = 2^2$$

$$x^2 + y^2 + 4 - 4y = 4$$

$$x^2 + y^2 - 4y = 0$$

∴ The equation of the circle is $x^2 + y^2 - 4y = 0$

2. Centre (-2, 3) and radius 4

Solution:

Given:

Centre (-2, 3) and radius 4

Let us consider the equation of a circle with centre (h, k) and

Radius r is given as $(x - h)^2 + (y - k)^2 = r^2$

So, centre (h, k) = (-2, 3) and radius (r) = 4

The equation of the circle is

$$(x + 2)^2 + (y - 3)^2 = (4)^2$$

$$x^2 + 4x + 4 + y^2 - 6y + 9 = 16$$

$$x^2 + y^2 + 4x - 6y - 3 = 0$$

 \therefore The equation of the circle is $x^2 + y^2 + 4x - 6y - 3 = 0$

3. Centre (1/2, 1/4) and radius (1/12)

Solution:

Given:

Centre (1/2, 1/4) and radius 1/12

Let us consider the equation of a circle with centre (h, k) and

Radius r is given as $(x - h)^2 + (y - k)^2 = r^2$

So, centre (h, k) = (1/2, 1/4) and radius (r) = 1/12

The equation of the circle is

$$(x - 1/2)^2 + (y - 1/4)^2 = (1/12)^2$$

$$x^2 - x + \frac{1}{4} + y^2 - \frac{y}{2} + \frac{1}{16} = \frac{1}{144}$$

$$x^2 - x + \frac{1}{4} + y^2 - \frac{y}{2} + \frac{1}{16} = \frac{1}{144}$$

$$144x^2 - 144x + 36 + 144y^2 - 72y + 9 - 1 = 0$$

$$144x^2 - 144x + 144y^2 - 72y + 44 = 0$$

$$36x^2 + 36x + 36y^2 - 18y + 11 = 0$$

$$36x^2 + 36y^2 - 36x - 18y + 11 = 0$$

 \therefore The equation of the circle is $36x^2 + 36y^2 - 36x - 18y + 11 = 0$

4. Centre (1, 1) and radius $\sqrt{2}$

Solution:

Given:

Centre (1, 1) and radius $\sqrt{2}$

Let us consider the equation of a circle with centre (h, k) and

Radius r is given as $(x - h)^2 + (y - k)^2 = r^2$

So, centre (h, k) = (1, 1) and radius (r) = $\sqrt{2}$

The equation of the circle is

$$(x-1)^2 + (y-1)^2 = (\sqrt{2})^2$$

$$x^2 - 2x + 1 + y^2 - 2y + 1 = 2$$

$$x^2 + y^2 - 2x - 2y = 0$$

∴ The equation of the circle is $x^2 + y^2 - 2x - 2y = 0$